

STATISTICAL METHODS

Practical Manual

Ist Semester, B. Fisheries Sciences



Compiled by

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Problems:

- 1. Calculation of Arithmetic Mean for Continuous Frequency Distribution**
- 2. Calculation of Median for Continuous Frequency Distribution**
- 3. Calculation of Mode for Continuous Frequency Distribution**
- 4. Calculation of Standard Deviation for Continuous Frequency Distribution**
- 5. Calculation of Pearson's Correlation Coefficient**
- 6. Calculation of Pearson's Correlation Coefficient**
- 7. Calculation of Spearman's Rank Correlation Coefficient**
- 8. Problem on Chi-Square Goodness of fit**

1) Calculate the mean for the following frequency distribution

Class Interval :	0-8	8-16	16-24	24-32	32-40	40-48
Frequency :	8	7	16	24	15	7

⇒ Solution: Here, we take $A = 28$ and $h =$

Computation of Mean

Class Interval	Mid-Value (x)	Frequency (f)	$d = \frac{x-A}{h}$	fd
24-32	28	24	0	0
32-40	36	15	1	15

$$\bar{x} = A + h \sum fd$$

$$28 + 8 \times (-25) \quad 28 \quad \underline{200} \quad 25.404.$$

2) Find the median wage of the following distribution

Wages (in Rs) : 2000-3000 3000-4000 4000-5000 5000-6000 6000-7000

of

Computation of median

Wages (in Rs)	No. of employees	c.f
1000 - 2000	5	8
2000 - 3000	10	28
3000 - 4000	10	
4000 - 5000		
5000 - 6000		
6000 - 7000		
		re

Cumulative frequency just greater than 21.5 is 28 and the corresponding class is 000 - 5000. Ans r o? a a T*

$$\text{Hence using median } \frac{4000 + 1000}{20} (21.5 - 8) = \frac{4000 + 675}{20} = 4675$$

3) Calculate mode for the following distribution:
Class Interval : 0-10 10-20 20-30 30-40 40-50 50-60 60-70

70-80

Thus, the class interval 40-50 is the modal class. Using mode formulae, the value of the mode is given by :

$$\text{Mode } 40 + \frac{10(28-12)}{(2 \times 28-12-20)} = 40 + \frac{10 \times 16}{40} = 46$$

4) Calculation of standard deviation for continuous frequency distribution

Age (in years) : 20-30 30-40 40-50 50-60 60-70 70-80 80-90

No. of members: 3 61 132 153 140 EI 2

Age group	Mid value (x)	Frequency (f)	$d = \frac{x-55}{10}$	fd	fd^2
20-30	25	3	-3	-9	27
30-40	35	61	2	-122	244
40-50	55	132	0	0	0
50-60	55	153	0	0	0
60-70	65	140	1	140	140
70-80	75	51	2	102	204
80-90	85	2	3	6	0

$$\bar{x} = A + h \frac{\sum fd}{N}$$

$$55 + 10 \times (-15) = 55 - 0.28 = 54.72 \text{ years.}$$

$$\sigma^2 = h^2 \left[\frac{1}{n} \sum (x_i - \bar{x})^2 \right] = 100 \left[\frac{765}{542} - (10.028)^2 \right]$$

$\therefore \sigma$ (Standard Deviation) = $\sqrt{141.07}$ 11.88 years.

5. Calculate the correlation coefficient for the following heights (in inches) for father's (x) and their sons (y).

x : 65 66 67 67 68 69 70 72

y : 67 68 65 68 72 72 69 71

65	67	4225	4489	4855
& Q	# i	# 8 &	f { 8 #	
80		\\$ 900	\\$ 8 #;	4830
# \$	# {	# } \$ \	30 # }	5112
Total	544	552	37028	37560

$$\bar{x} = \frac{1}{n} \sum x = \frac{544}{8} = 68 \quad \bar{y} = \frac{1}{n} \sum y = \frac{37560}{8} = 4695$$

$$r(x,y) = \frac{\text{cov}(x,y)}{\sigma_x \sigma_y} = \frac{\frac{1}{n} \sum xy - \bar{x} \bar{y}}{\sqrt{(\frac{1}{n} \sum x^2 - \bar{x}^2)(\frac{1}{n} \sum y^2 - \bar{y}^2)}}$$

$$\frac{\frac{1}{8} \times 37560 - 68 \times 69}{\sqrt{- \{ \{ \frac{1}{8} \times 552 - 68^2 \} \} \{ \frac{1}{8} \times 4695 - 69^2 \}}}$$

$$\frac{4695 - 4692}{\sqrt{4695 - 4692}} = \frac{3}{\sqrt{3}} = \frac{1}{\sqrt{3}}$$

6) The ranks of same 16 students in Mathematics and Physics are as follows. Two numbers within brackets denote the ranks of the

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 (10,11) (11,15) (12,9) (13,14) (14,12) (14,12) (15,16) (16,13)

Calculate the rank correlation coefficient for preferences of this group in Mathematics and Physics.

Maths (x)	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
Ranks in Physics (y)	1 10 3 4 5 7 2 6 8 11 15 9 14 12 16 13
$d = x - y$	0 -8 0 0 0 -1 5 2 1 -1 -4 3 -1 2 -1 3

$$\text{Total } (d^2) = 136$$

∴ Rank correlation coefficient is given by :

$$r = \frac{6 \sum d^2}{n(n^2 - 1)} = \frac{6 \times 136}{16 \times 255} = 1 - \frac{1}{5} = \frac{4}{5} = 0.8$$

7) Find the equation of the least square straight line (considering x as independent variable) using the following data:

4	4	16	16	/g
8	5	64	40	25
11	8	121	88	64
$= \sum x$	56	40	524	364
				251

Therefore, the normal equation is

$$40 = 8a + 56b$$

$$364 = 56a + 524b.$$

Finding the solution of the above equations we get,

$$a = \frac{6}{11}, b = \frac{7}{11}$$

∴ The equation of least square std. line is

8) Test the hypothesis that the number of parts demanded does not depend on the day of the week. (Given, the values of chi-square significance at 5, 6, 7 d.f are respectively 11.07, 12.59, 14.07, at the 5% level of

"^o CUE "or $V^A \cdot 01 < Z^A \cdot 05$ " • . . $V^A \cdot 01$ yr
number of parts demanded does not depend on the day of week.

Under the null hypothesis, the expected frequencies of the spare part demanded on each of the six days should be :-
$$\bar{d} = (1124 + 1125 + 1110 + 1120 + 1126 + 1115)$$

Days	frequency		$(f_i^o - e_i)$	$\frac{e_i}{e_i}$
	Observed (f_i)	Expected (e_i)		
Mon	1124	1120	16	0.014
Tues	1125	1120	25	0.022
Wed	1110	1120	100	0.089
Thurs	1120	1120	0	0
Fri	1126	1120	36	0.032
Sat	1115	1120	25	0.022
Total	6720	6720		0.149

$$\chi^2 = \sum \frac{(f_i^o - e_i)^2}{e_i}$$

The number of degrees of freedom = 6-1 = 5 (since we are given 6 frequencies subjected to only one linear constraint)

$$\sum f_i^o = \sum e_i^o = 6720$$

The tabulated $\chi_{0.05}^2$ for 5 d.f = 11.07

Since calculated value of χ^2 is less than the tabulated value it is not significant and the null hypothesis may be accepted at 5% level of significance. Hence we conclude that the numbers of pants demanded are same